

Hannes Rieser
Faculty of Linguistics and Literary Studies
Bielefeld University, Germany

A Process Algebra Account of Speech-Gesture Interaction.
Revised and Extended Version

CLASP, Gothenburg University
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2. Speech-gesture Asynchrony: Stimulus, Cave-Data, Dialogue Example, Annotation
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5. A λ - ψ -modelling of the Dialogue Example Capturing Incrementality and Semantic Scope
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Introduction and Idea of Paper

Facts (SaGA rated corpus-data, Lücking et al. 2012):

Iconic and referential gestures

- are semantically related with the speech they accompany
- do not perfectly synchronize with semantic coordination point in speech
 - *contra* McNeill (1992)
 - modern speech-gesture interaction research (Alahverdzhieva and Lascarides 2010, Giorgolo (2010), Lascarides, A. and Stone, M. 2009, Lücking 2013, Röpke 2011, Röpke, Hahn, and Rieser 2013 among others) has not developed general solutions for this problem
- come before relevant speech, after it or overlap
- can be independent/provide independent content

Introduction and Idea of Paper

Claim: description of speech-gesture coordination cannot be given solely in a naïve compositional way

Caveat: composition does play a role finally, when the speech-gesture contact points have been identified

Given asynchrony, a lot of work has to be done before the speech-gesture contact points are identified.

Parallel problem also treated here: incrementality and scope resolution

Introduction and Idea of Paper

Proposed solution for the asynchrony problem:

- view gesture and speech as independent processes interacting if semantically apt
- move to methodology working with a process ontology instead of a purely domain-of-objects one as in model theory used: ψ -calculus (Johansson, 2010, Bengtson et al. 2011)
- Process Algebra
 - recent extension of Milner's π -calculus (Milner, 1999, Parrow, 2001, Sangiorgi and Walker, 2001),
 - works with processes (agents) and data structures
 - transmitted between agents *via* structured channels using input-output facilities

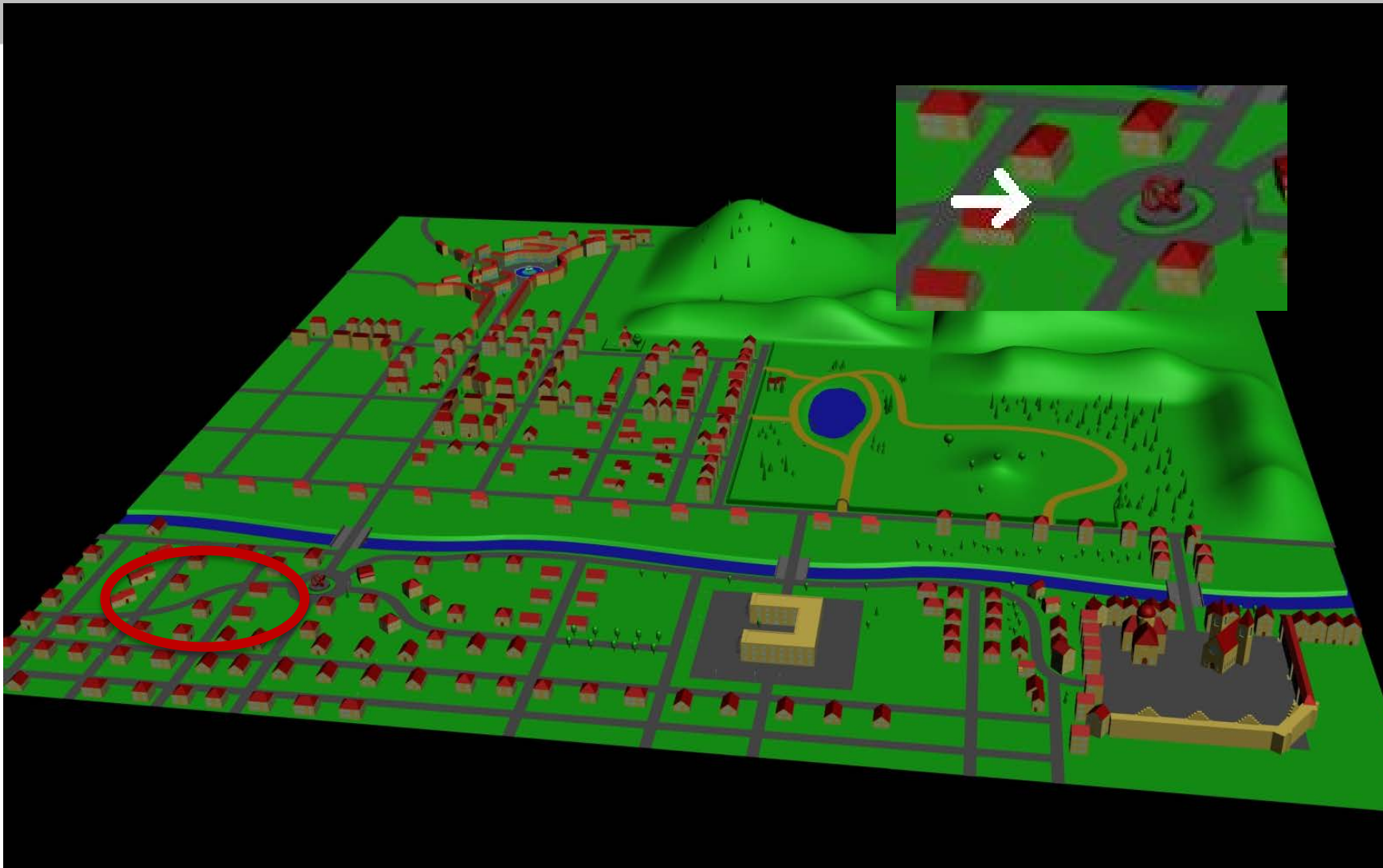
Aside: gesture and speech are NOT bisimilar processes, no identity

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Speech-gesture Asynchrony

Stimulus: VR-rendering of domain model for route-description dialogues



Speech-gesture Asynchrony

Stimulus: VR-rendering of domain model for route-description dialogues



Speech-gesture Asynchrony

1 Route-g. Ok, well the tour starts and yes it is such a wormed street follow it
 2 | - WINDING-GESTURE_{RG} - |
 3 Follower Yes
 4
 5 Route-g. And then there is a sculpture it is kind of red looks like two intertwined pretzels
 6 | -TWO-BRETZELS GESTURE_{RG} - |
 7 Follower
 8
 9 Route-g. or so
 10
 11 Follower aha
 12
 13 Route-g. Towards it and it is kind of round and it goes in a circle well there is a circle
 14 | - GESTURE_{RG} - | | - GESTURE_{RG} - | | - GESTURE_{RG} - |
 15 around it
 16
 17 Follower Yes
 18
 19 Route-g. And then one passes its right side
 20 | - GESTURERG - | | - GESTURERG - | BODY MOVE TO PANTOMIME ONLOOKER POSITION
 21 AND DIRECTIONS ABORTED
 22 Follower Hold on well you-CUT OFF well you walk now
 23 | - WINDING-GESTURE_F - ----
 24 into this street and then where is the sculpture is it at the front or to the
 25 ----- | - WINDING-GESTURE-HELD -----
 | -GESTURE_{F-LH}- | | -GESTURE_{F-LH}- | | -GESTURE_{F-LH}- | | -GESTURE_{F-LH}- |
 26 right
 27 - winding-gesture-held -----
 | -GESTURE_{F-LH}- |
 28 Route-g. Yes it comes at you notice it immediately
 29 | - TWO-HANDED-GESTURE_{RG} - |
 30 Follower OK
 31 - WINDING-GESTURE-HELD -----
 32 Route-g. When you notice the wormed street.
 33 | - WINDING GESTURE - |
 34 Follower OK
 35 - WINDING-GESTURE-HELD -----

Speech-gesture Asynchrony: Stimulus, Cave-Data, Dialogue Example, Annotation



Speech-gesture Asynchrony

Dialogue Example (Route description V16, SaGA-Corpus)

22 Follower Hold on well you-CUT OFF well you walk now
 23 | - WINDING-GESTURE_F - - - -

24 into this street and then where is the sculpture is it at the front or to the
 25 - - - - - | - WINDING-GESTURE-HELD - - - - -
 | -GESTURE_{F-LH} - | | -GESTURE_{F-LH} - | | -GESTURE_{F-LH} - | | -GESTURE_{F-LH} - |

26 right
 27 - winding-gesture-held - - - - -
 | -GESTURE_{F-LH} - |

28 Route-g. Yes it comes at you notice it immediately
 29 | - TWO-HANDED-GESTURE_{RG} - |

30 Follower OK
 31 - WINDING-GESTURE-HELD - - - - -

32 Route-g. When you notice the wormed street.
 33 | - WINDING GESTURE - |

34 Follower OK
 35 - WINDING-GESTURE-HELD - - - - -

Speech-gesture Asynchrony: Stimulus, Cave-Data, Dialogue Example, Annotation



Speech-gesture Asynchrony: Stimulus, Cave-Data, Dialogue Example, Annotation

The screenshot displays the ELAN 4.9.3 interface for file 'V16_Feinannotation.eaf'. It features a video player with three camera views of a dialogue between two individuals. The interface includes a menu bar (Datei, Bearbeiten, Annotation, Zeile, Typ, Suche, Ansicht, Optionen, Fenster, Hilfe) and a toolbar with playback controls. A control panel on the right shows volume settings (Lautstärke) and speed settings (Geschwindigkeit) for three video tracks (V16K1.mov, V16K2.mov, V16K3.mov). The main area is a timeline with a scale from 00:00:30.000 to 00:00:44.000. The timeline contains several tracks of annotations:

- F.G.Sequence** (red): discourse, iconic
- F.G.Right.Phra** (green): prep stroke, post.hold, retr
- F.G.Right.Ph** (green): B-spread
- F.G.Right.** (green): 0
- F.G.Right.** (green): 0
- F.G.Right.** (green): 0
- F.G.Right.** (green): 0
- F.G.Right.** (green): PTB/PTL>PTB>PTL>PT
- F.G.Right.** (green): LINE
- F.G.Right.** (green): ML>MR>ML>MR
- F.G.Right.** (green): Vollbild ausschneiden
- F.G.Right.** (green): 0
- F.G.Right.** (green): BAB/BTL>BTL>BAB>BA
- F.G.Right.** (green): 0

ELAN-annotation of central example (still)

Speech-gesture Asynchrony: Stimulus, Cave-Data, Dialogue Example, Annotation

Observations

Follower's contribution:

- winding gesture starts with “well” line (22) and continues up to “street” and is held until line (34)
- no verbal indication of street's bends, instead Follower's winding gesture plus the word “street”
- the two information processes/agents together produce multi-modally “wormed street”/”geschlängelte Straße”

Route-giver's contribution:

- Uses a winding gesture in lines 2 and 33.

Gestural “contact” in lines 31 to 35:

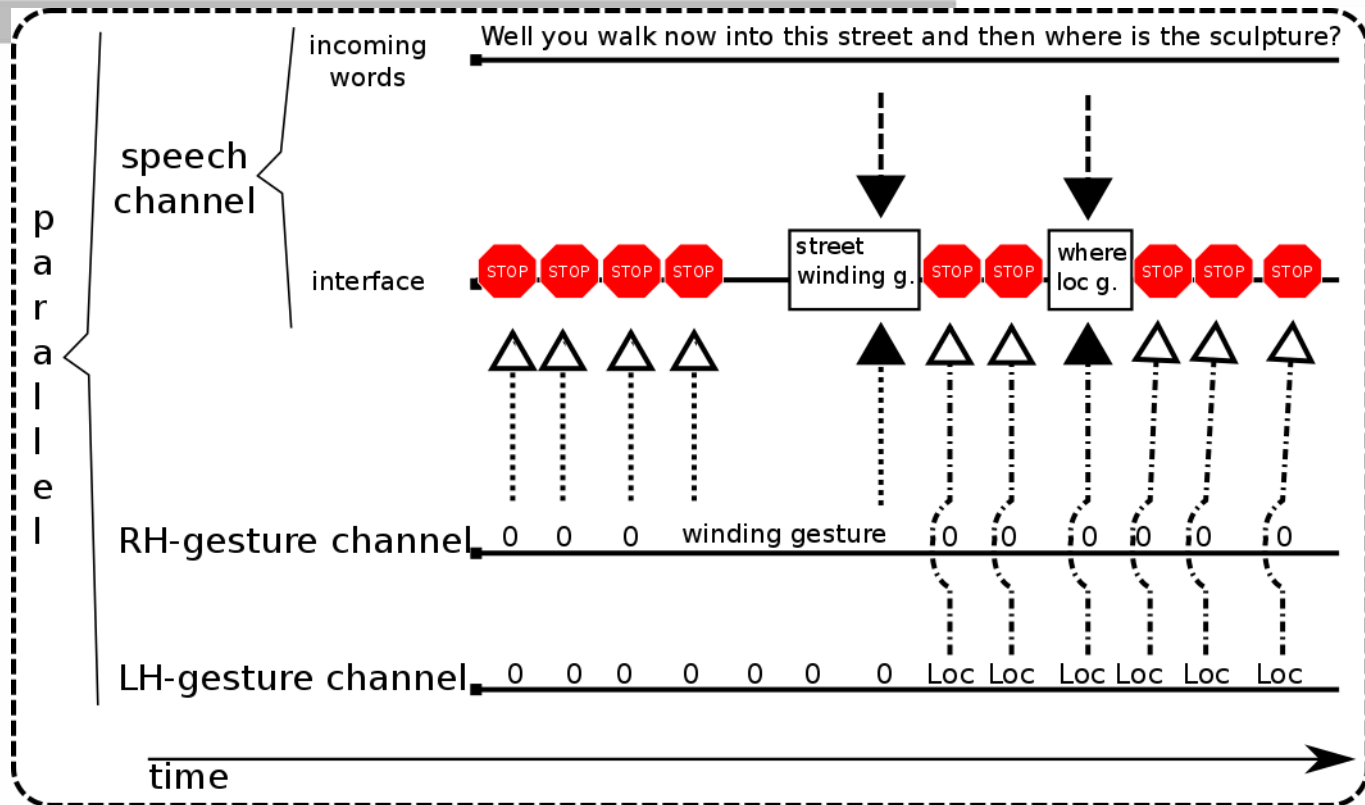
- Follower holds the winding gesture
- Route-g. produces a winding gesture

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Speech-gesture Asynchrony: Solution Intuitions

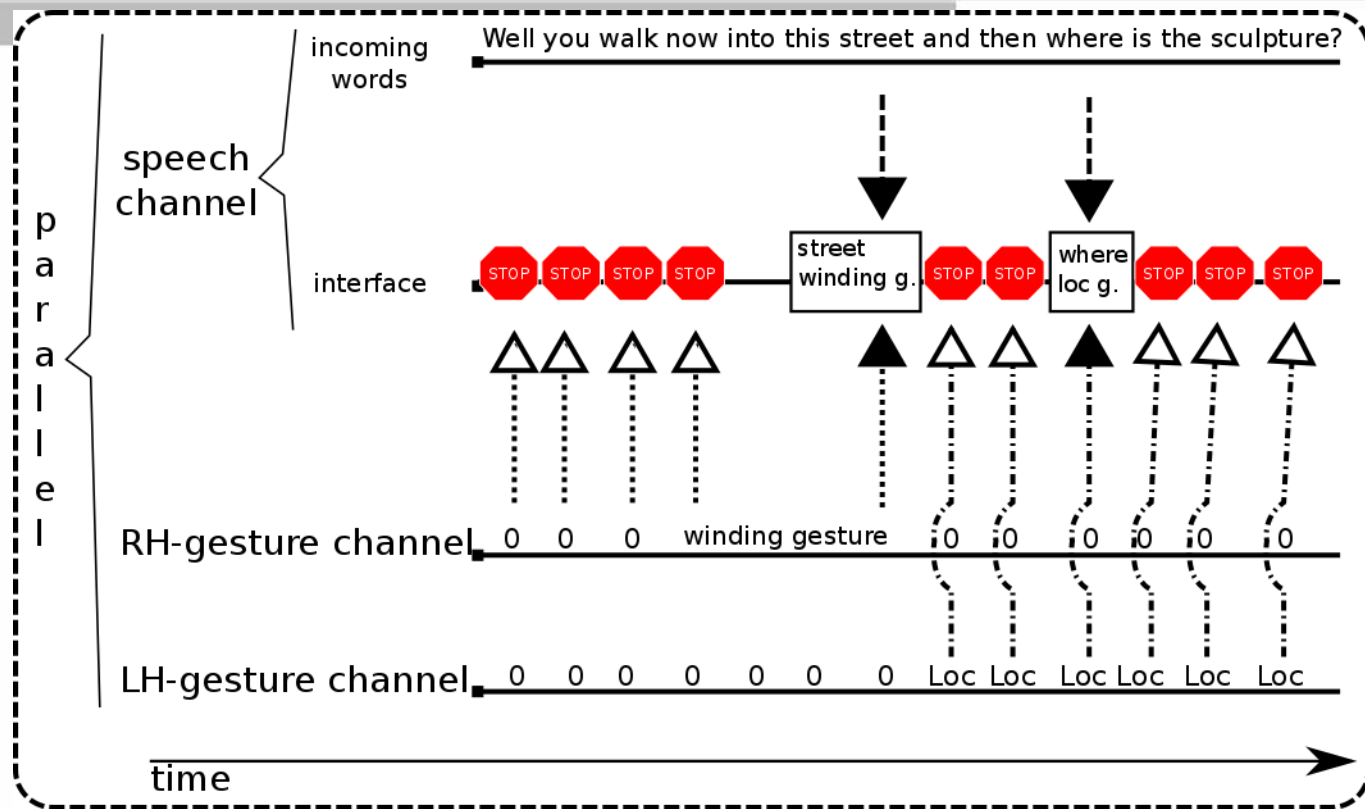
Didactic picture of channel interaction between speech and gesture



The winding gesture is taken to cooperate with the noun "street" (preferred reading).

Speech-gesture Asynchrony: Solution Intuitions

Didactic picture of channel interaction between speech and gesture

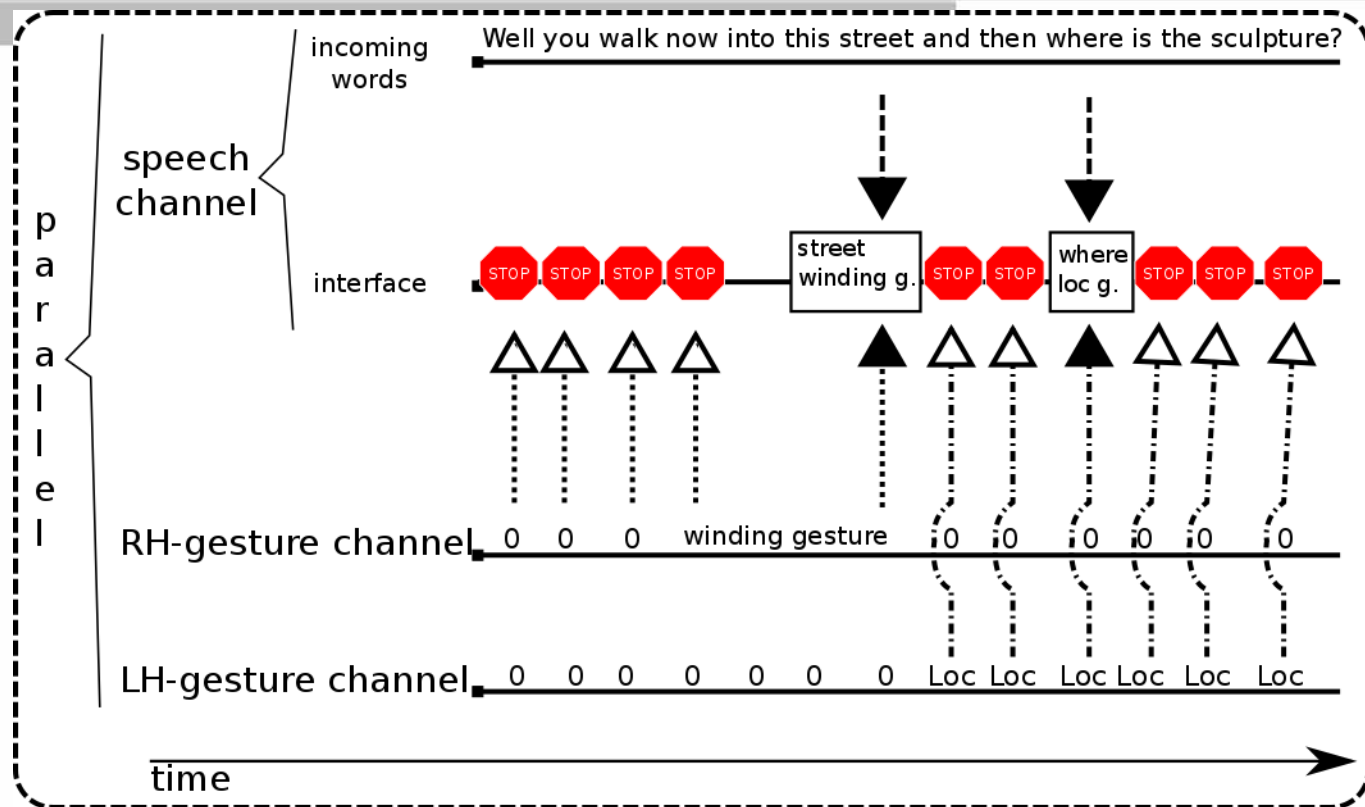


Assumptions:

- channels for speech, LH- and RH-gesture
- independent production of information on channels speech, RH, and LH

Speech-gesture Asynchrony: Solution Intuitions

Didactic picture of channel interaction between speech and gesture

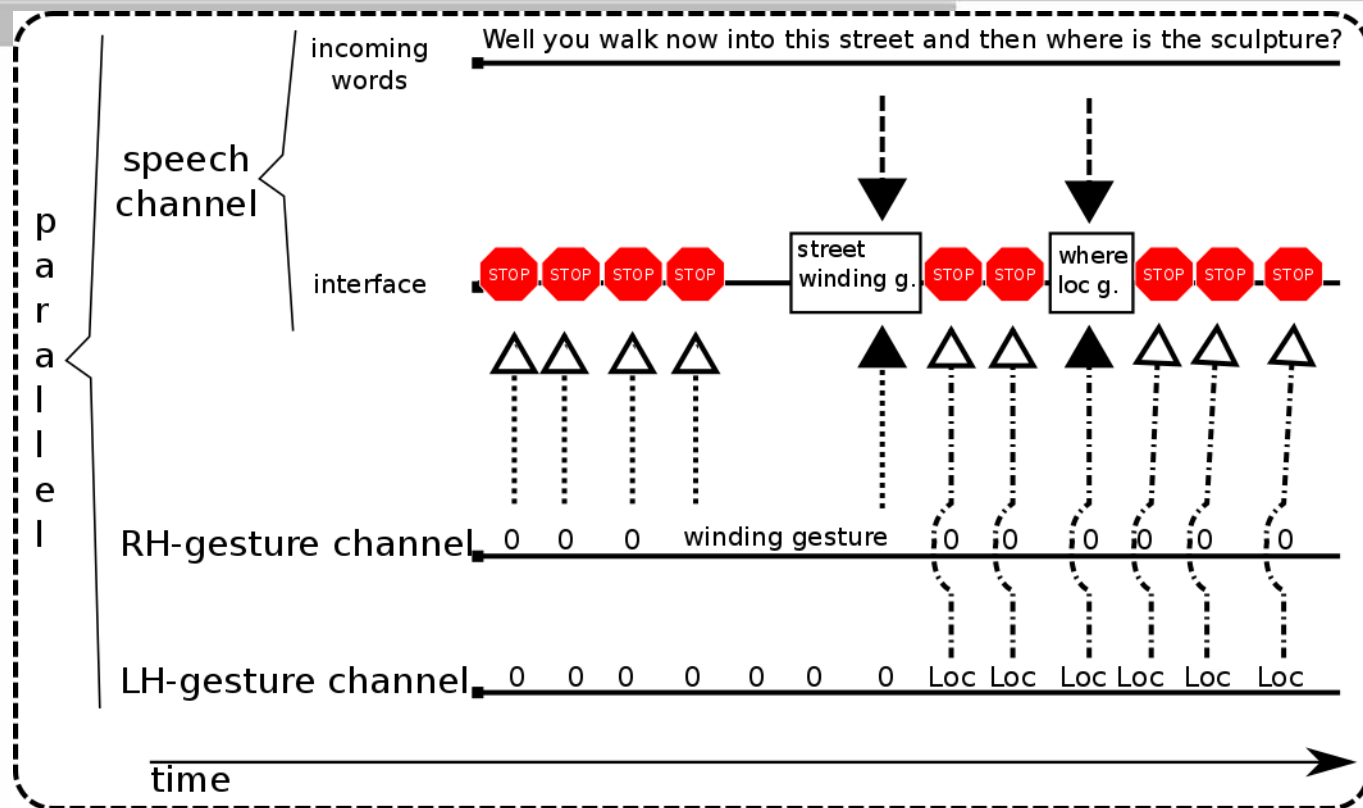


Assumptions:

- winding gesture's stroke information denied access to interface channel
- winding gesture waits until it can interact

Speech-gesture Asynchrony: Solution Intuitions

Didactic picture of channel interaction between speech and gesture

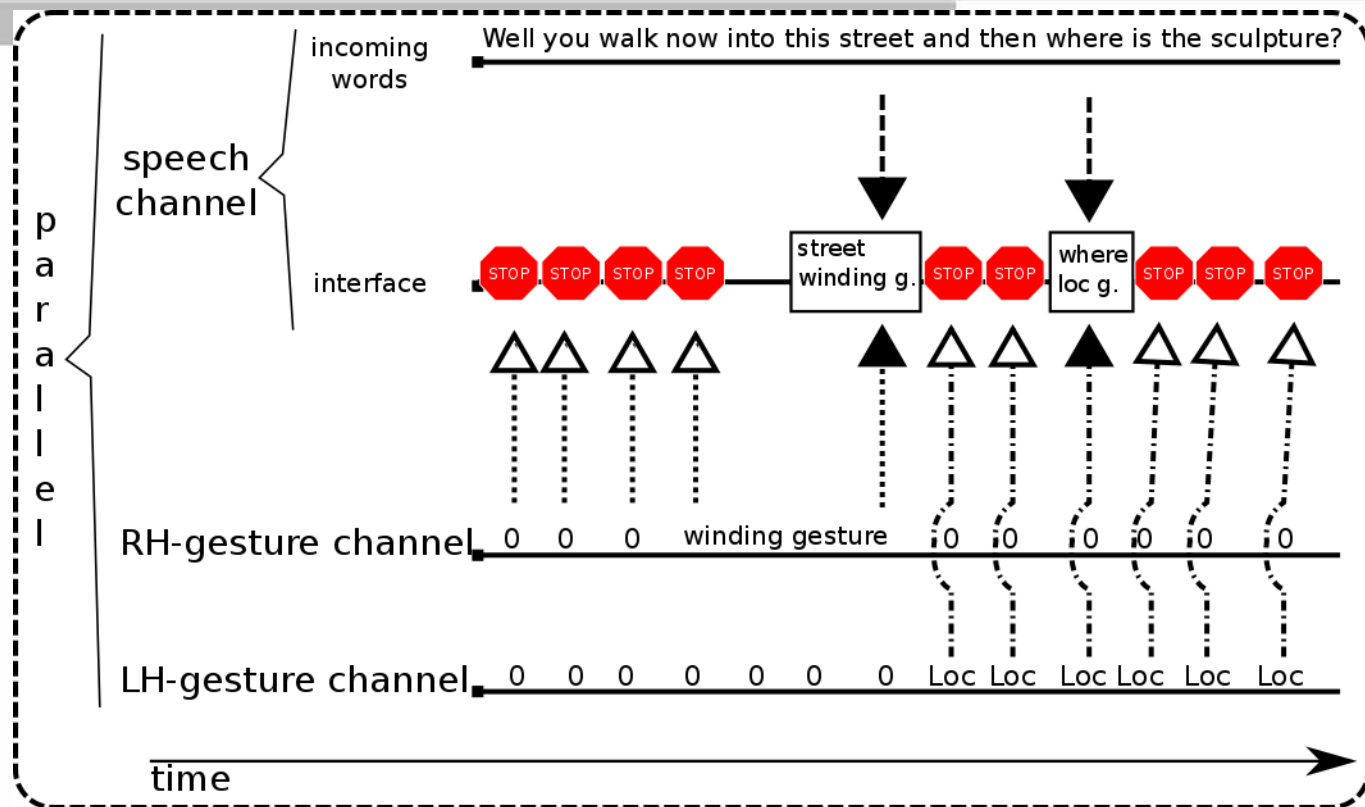


How done?

- access properties of winding gesture's and "street"'s semantics implemented by typing
- here Montague grammar/typed λ -calculus, alternatives: Combinatory Logics, HPSG's AVMS, other typing regimes

Speech-gesture Asynchrony: Solution Intuitions

Didactic picture of channel interaction between speech and gesture

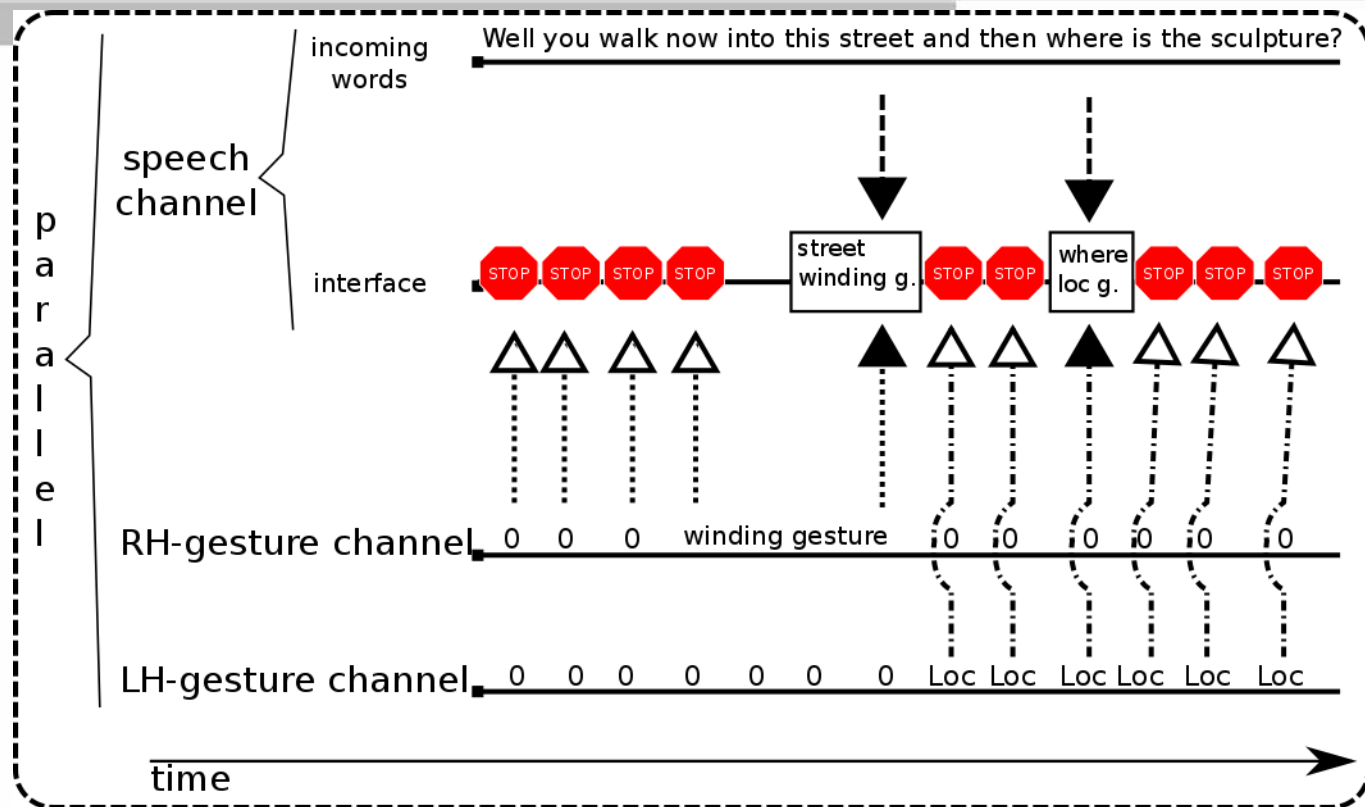


Assumptions:

- after the interaction, winding gesture's interfacing possibilities are set to 0.

Speech-gesture Asynchrony: Solution Intuitions

Didactic picture of channel interaction between speech and gesture



Technical problem:

- Fuse channel technology and typed λ -calculus

Attempted in my λ - ψ -hybrid calculus

Speech-gesture Asynchrony: Solution Intuitions

Cooper's Conjecture: The Event Case

R. Cooper's idea (Ghent July 2016):

- What the Follower has in mind is the event of walking into the street.
- Gesture indicates a property of the event.
- Event going in bends.

Accounts for the length of the stroke: from “you” to “into” (“Du” ...”rein”).

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ψ -calculus Essentials and How to Capture the Main Intuitions with them

Recap and Outlook

Empirical observations provide evidence for

- channels on which information (data, agents or procedures) can be sent
- processes operating concurrently
- communication among processes and
- indication when a process is active (waits, acts) or comes to its end

Communication: organised mainly with

- input- output mechanism
- parallel processes

Blocking of information:

- achieved with typing of data structures and processes.

ψ -calculus Essentials and How to Capture the Main Intuitions with them

What do we have in Process Algebra ψ to model these intuitions?

We have parameters, operators on these, frames and agents.

ψ -calculus Essentials and How to Capture the Main Intuitions with them

Parameters indicating data types given in definition 1

Definition 1

T the (data) terms, ranged over by M, N

C the conditions, ranged over by φ

A the assertions, ranged over by (capital) Ψ

(Bengtson et al. 2011, pp. 4-14)

Data terms:

- can come from any (higher order) logic
- here typed λ -calculus chosen
- reasons:
 - semantics tradition
 - well researched into model- and proof-theoretically (cf. Barendregt et al. 2013, Cresswell 1973)
 - developing hybrid λ - ψ -functor-argument-structures

ψ -calculus Essentials and How to Capture the Main Intuitions with them

The equivariant operators come in definition 2

(“equivariance” for capturing α -equivalence)

Definition 2

$\leftrightarrow: T \times T \rightarrow C$

Channel Equivalence

$\otimes: A \times A \rightarrow A$

Composition

$\vdash \subseteq A \times C$

Entailment

ψ -calculus Essentials and How to Capture the Main Intuitions with them

The ψ -calculus agents/processes, indicated by P, Q, \dots

Definition 3

0	Inert agent
$\overline{M}N.P$	Output process
$\underline{M}(\lambda x)N.P$	Input process, written as “ $\underline{M}(x)N.P$ ”
τ	Silent agent
$\text{case } \varphi_1: P_1 \parallel \dots \parallel \varphi_n: P_n$	Case construct
$(\nu a)P$	Restriction on process P
$P \mid Q$	Parallel processes
$!P$	Replication process: $!P =_{\text{def}} P \mid !P$
(Ψ)	Assertion
\cdot	Compositional operator
Auxiliary symbols:	
\langle, \rangle	Brackets enclosing typed λ -expressions

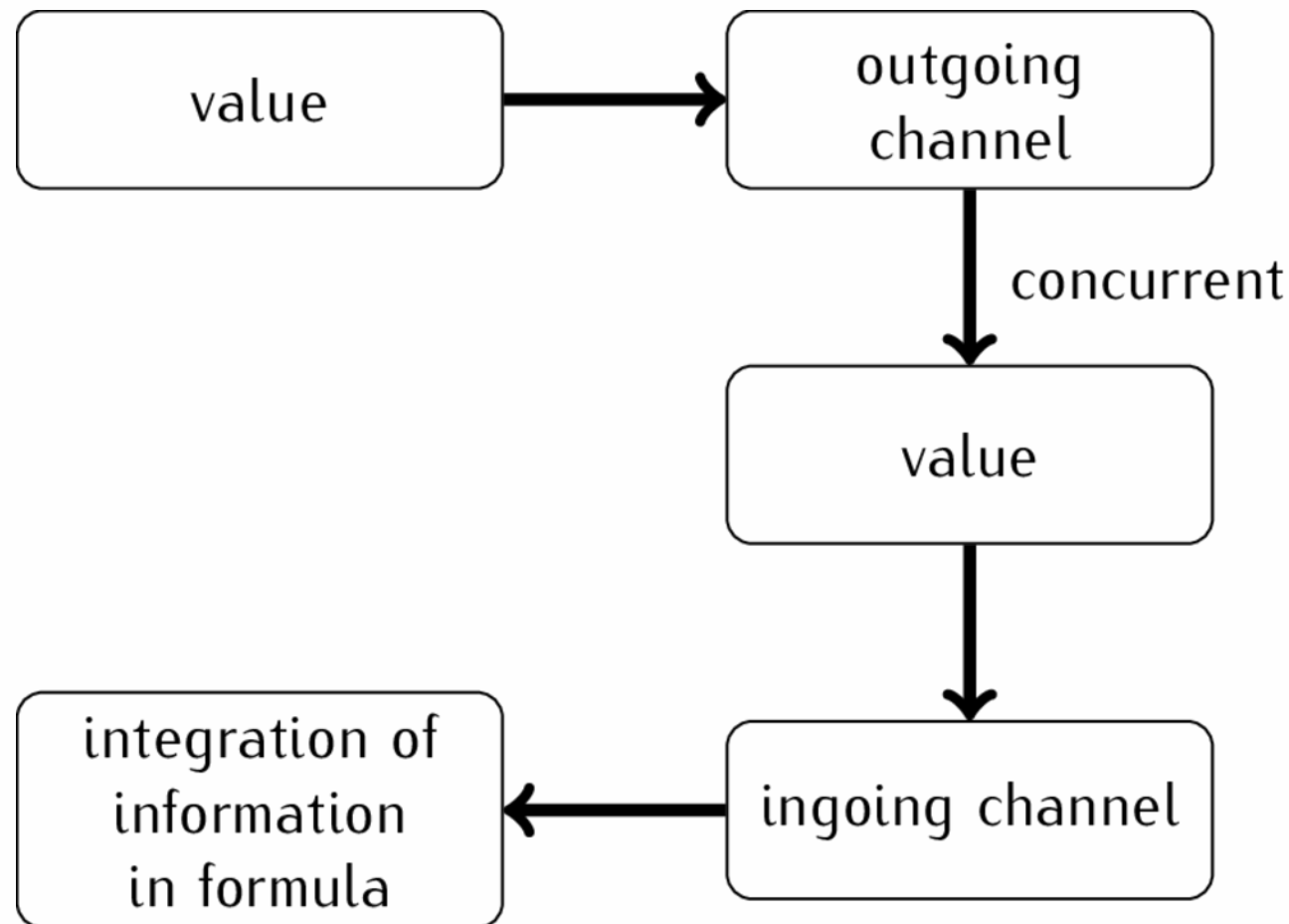
ψ -calculus Essentials and How to Capture the Main Intuitions with them

The ψ -calculus agents/processes, indicated by P, Q...

Mainly used in this talk: 0 agent, $\overline{M}N.P$, $\underline{M}(x)N.P$, $P \mid Q$, $!P$, “.”

ψ -calculus Essentials and How to Capture the Main Intuitions with them

i-o-facility through Channel Communication



ψ -calculus Essentials and How to Capture the Main Intuitions with them

Structural Operational Semantics for Parallel Agents

Transition Rules:

Schema

premises

conclusion

COM (simplified)

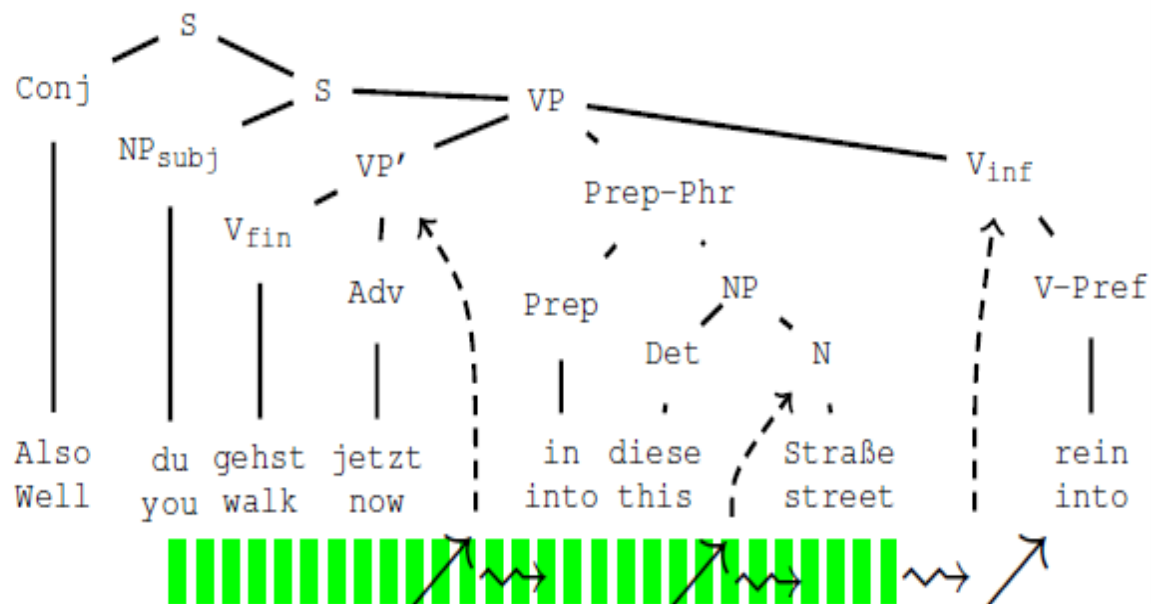
$$\frac{P \xrightarrow{\bar{a}b} P' \quad Q \xrightarrow{ab} Q'}{P|Q \xrightarrow{\tau} P'|Q'}$$

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A λ - ψ -modelling of the Dialogue Example

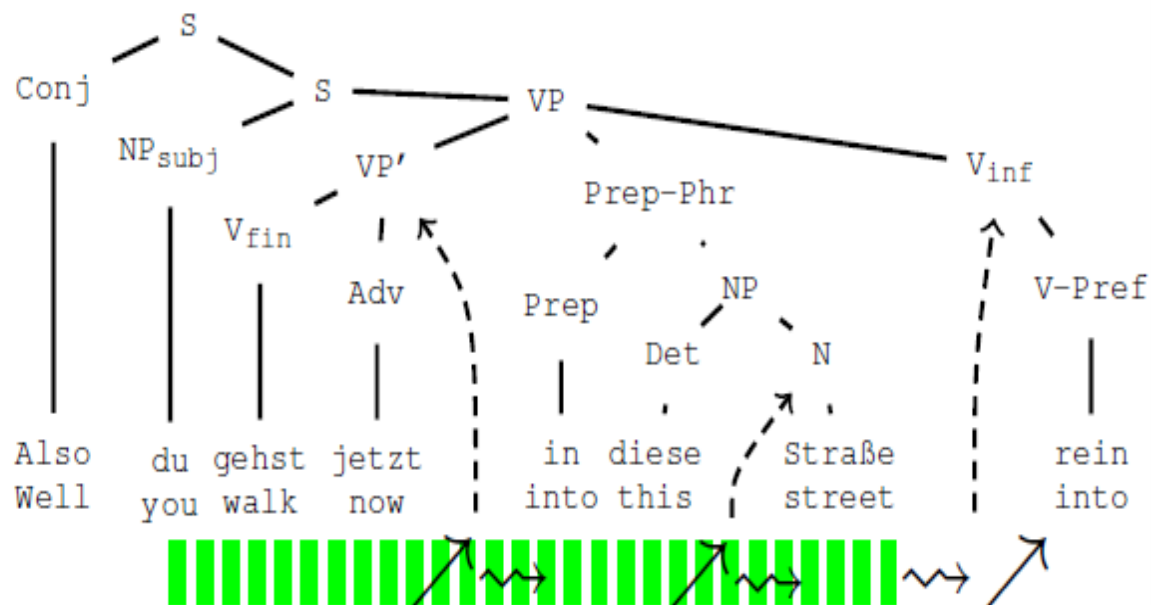
Empirical Foundations



- Syntax of the Follower's clarification request
- Winding gesture starts before possible integration points with speech and continues afterwards
- Gesture stroke: marked with a green dashed line

A λ - ψ -modelling of the Dialogue Example

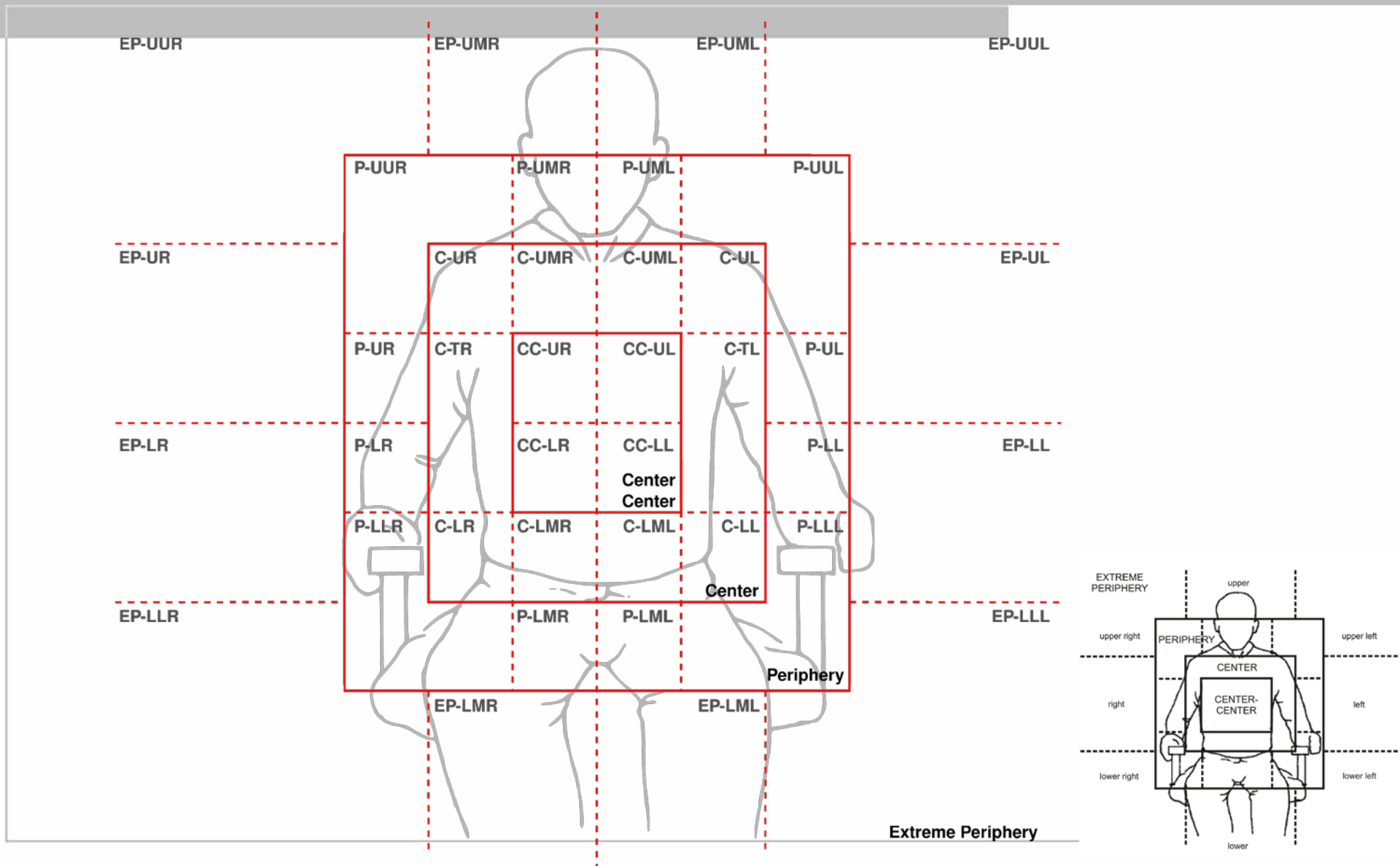
Empirical Foundations



- Syntax structure: “German Satzklammer” (didactic English translation)
- Possible speech-gesture interface points “walk now”, “street” and “into”: marked with dashed arrows
- Winding arrow: indicates winding of gesture.

A λ - ψ -modelling of the Dialogue Example

Empirical Foundations



A λ - ψ -modelling of the Dialogue Example

Empirical Foundations

F.Right.Hand.Shape		B-spread
F.Right.Palm.Direction		PTB/PTL>PTB>PTL>PTB>PTB/PTL
F.Right.Palm.Movement		LINE
F.Right.Path.of.Palm.Direction		ML>MR>ML>MR
F.Right.Back.of.Hand.Direction		BAB/BTL>BTL>BAB>BAB/BTL

F.Right.Path.of.Wrist.Location		LINE
F.Right.WL.Movement.Direction		MF/ML
F.Right.Wrist.Position		C-RT
F.Right.Wrist.Distance		D-CE

Follower's AVM of gesture annotation. Represented is stroke of gesture.
Translated as "winding"

A λ - ψ -modelling of the Dialogue Example

Empirical Foundations

RG.Right.Hand.Shape	B-spread	
RG.Right.Palm.Direction	PTL>PTB/PTL>PTL	
RG.Right.Back.of.Hand.Direction	BAB>BAB/BTL>BAB/BUP	
RG.Right.PathOfBack.of.Hand.Direction	MF>ML>MF>MR/MU	

RG.Right.Wrist.Position	CC	
RG.Right.Wrist.Distance	D-CE	

Routegiver's AVM of first winding-gesture annotation. Represented is stroke of gesture. Translated as "winding"

A λ - ψ -modelling of the Dialogue Example

Empirical Foundations

RG.Right.Hand.Shape		B-spread
RG.Right.Palm.Direction		PTB/PTL>PTL>PTL
RG.Right.Path.Of.Palm.Direction		ARC
RG.Right.Back.of.Hand.Direction		BAB/BTL>BAB
RG.Right.Path.Of.Back.of.Hand.Direction		ARC>LINE
RG.Right.Back.of.Hand.Movement.Direction		MF>ML>MF>MR/MU
RG.Right.Path.Of.WristLocation		LINE>LINE
RG.Right.WristLocation.MovementDirection		ML>MF
RG.Right.Wrist.Position		CC
RG.Right.Wrist.Distance		D-CE

Routegiver's AVM of second winding-gesture annotation. Represented is stroke of gesture. Translated as "winding"

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A λ - ψ -modelling of the Dialogue Example

The λ - ψ -calculus Tailored to Suit

well

you

walk

now

into

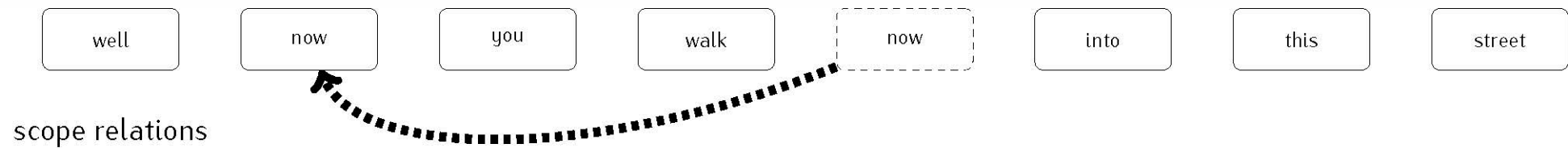
this

street

incoming words

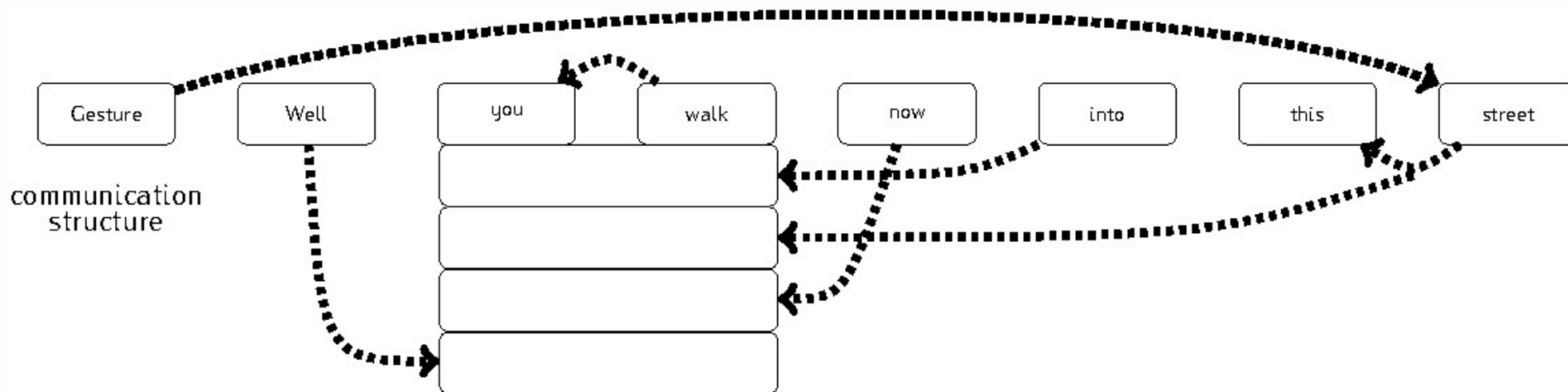
A λ - ψ -modelling of the Dialogue Example

The λ - ψ -calculus Tailored to Suit



A λ - ψ -modelling of the Dialogue Example

The λ - ψ -calculus Tailored to Suit



A λ - ψ -modelling of the Dialogue Example

The λ - ψ -calculus Tailored to Suit

Problem: Respect the order of the incoming gesture and words and model correct scope relations

The λ - ψ -calculus Tailored to Suit:

Definitions 1-3 in section 4 define a family of ψ -calculi with various open slots

A λ - ψ -modelling of the Dialogue Example

The λ - ψ -calculus Tailored to Suit

Now: set up a λ - ψ -calculus to model the asynchronous speech-gesture communication of the dialogue example

Cresswellian type structure

$$T =_{\text{def}} N \cup \text{Var} \in \text{Cat}_i = \{p_{\langle 0,0 \rangle}, u_1, f_{\langle 0,1 \rangle}, f'_{\langle 0,e,1 \rangle}, r_{\langle 0,e',1 \rangle}, pr_{\langle 0,0 \rangle}\} \cup \\ \{e_1, e'_1, \text{winding}'_{\langle 0,1 \rangle}, \text{well}'_{\langle 0,0 \rangle}, \text{you}'_1, \text{walk}'_{\langle 0,e,1 \rangle}, \text{now}'_{\langle 0,0 \rangle}, \text{into}'_{\langle 0,e',1 \rangle}, \\ \text{this}'_{\langle 1,\langle 0,1 \rangle,1 \rangle}, \text{street}'_{\langle 0,1 \rangle}\} \cup \text{Var} \in C$$

$$C =_{\text{def}} \{fb_{\langle 0,\langle 0,1 \rangle,1 \rangle} \leftrightarrow b_{\langle 0,\langle 0,1 \rangle,1 \rangle} \leftrightarrow b'_{\langle 0,\langle 0,1 \rangle,1 \rangle}, we_{\langle 0,0 \rangle} \leftrightarrow we'_{\langle 0,0 \rangle}, w_{\langle 0,e,1 \rangle} \leftrightarrow \\ w'_{\langle 0,e,1 \rangle}, i_{\langle 0,e',1 \rangle} \leftrightarrow i'_{\langle 0,e',1 \rangle} \leftrightarrow in_{\langle 0,e',1 \rangle}, ts_1 \leftrightarrow ts'_1, nw_{\langle 0,0 \rangle} \leftrightarrow nw'_{\langle 0,0 \rangle} \leftrightarrow n_{\langle 0,0 \rangle}, \\ s_{\langle 0,1 \rangle} \leftrightarrow s'_{\langle 0,1 \rangle}\}$$

$$A =_{\text{def}} \{1\}$$

$$\otimes =_{\text{def}} \lambda \Psi 1, \Psi 2. 1$$

$$1 \vdash \{x \leftrightarrow y \mid x, y \in C \text{ and } x, y \in \text{Cat}_i\}$$

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News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

What the Speech-Gesture-Interaction Agent SGIA does:

- handles incrementality
- implements the intuitively correct scopes
- achieves the speech-gesture integration to produce a multi-modal meaning

News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \langle \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u)) e) w' \rangle i' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \langle \lambda g (\text{this}' x (g(x))) s' . 0 \rangle \mid \underline{b} (b'). \overline{s}. \langle b' \langle \lambda x (\text{street}'(x)) \rangle \rangle . 0$$

How SGIA works:

- Winding gesture: produced concurrently with the words <“well”, “you”, “walk”, “now”, “into”, “this”, “street”>

News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u)) e) w' \rangle i' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \langle \lambda g (\text{this}' x (g(x))) s' \rangle . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- Composable winding gesture representation sends its information to “street”, yielding “winding street”:

$$\underline{b} (b'). \overline{s}. \langle b' \langle \lambda x (\text{street}'(x)) \rangle \rangle . 0$$

$$\underline{b} (b'). \overline{s}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \lambda x (\text{street}'(x)) \rangle . 0$$

$$\underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u)) e) w' \rangle i' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- Property “winding street” sends its information to “this” and we get the referring expression “this winding street”:

$$\underline{s} (s'). \overline{ts}. \lambda g (\text{this}' x (g(x))) \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) . 0$$

$$\underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0$$

News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

“Street” solution

$SGIA =_{\text{def}} !\overline{fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w}$
 $(w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x,$
 $u))e)w' > i' > ts' > . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x$
 $(\text{street}'(x) \wedge \text{winding}'(x)). 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$

How SGIA works:

- Information tied to “you”: propositional function:

$\mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x,$
 $u))e)w' > i' > ts' > . 0$

News from λ - ψ : The Speech-Gesture-Interaction Agent SGIA

“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u))e)w' \rangle i' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

needs a lot of constant information

- a relation “walk” defined on an event e and a subject “you”:

$$\mid \overline{w}. \langle \text{walk}' \rangle . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u)) e) \text{walk}' > i' > ts' > . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

needs a lot of constant information

- a relation “walk” defined on an event e and a subject “you”

$$\mid \overline{w}. \langle \text{walk}' \rangle . 0$$

$$\underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda f \lambda ru (\lambda x (f(x, \text{you}') \wedge r(x, u)) e) \text{walk}' > i' > ts' > . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))e) \ggg \gg i' \gg ts' \gg . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

needs a lot of constant information

- a relation “walk” defined on an event e and a subject “you”

$$\mid \overline{w}. \langle \text{walk}' \rangle . 0$$

$$\underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))e) \ggg \gg i' \gg ts' \gg . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))) e \rangle \text{into}' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

$$\mid \overline{w}. \langle \text{walk}' \rangle . 0$$

$$\underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))) e \rangle \text{into}' \rangle ts' \rangle . 0$$

$$= \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))) e \rangle \text{into}' \rangle ts' \rangle . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))) e \rangle \text{into}' \rangle ts' \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- a relation “into” defined on an event e :

$$\overline{in}. \text{into}' . 0$$

$$\underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll \lambda ru (\lambda x (\text{walk}'(x, \text{you}') \wedge r(x, u))) e \rangle \text{into}' \rangle ts' \rangle . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \langle \lambda u (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, u)) e) \rangle \rangle \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- a relation “into” defined on an event e :

$$\overline{in}. \text{into}' . 0$$

$$\underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \langle \lambda u (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, u)) e) \rangle \rangle \rangle . 0$$

$$\gg ts' \rangle . 0$$

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“Street” solution

$SGIA =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w}$
 $(w'). \underline{i} (i'). \underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. nw' \ll \lambda u (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, u)) e$
 $\gg \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}.$
 $\text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge$
 $\text{winding}'(u)) \rangle . 0$

How SGIA works:

- the referring expression “this winding street”

$\overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0$

$\underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. nw' \ll \lambda u (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, u)) e \langle \text{this}' x$
 $(\text{street}'(x) \wedge \text{winding}'(x)) \gg . 0$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle .0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \langle \lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))) e \rangle \rangle \rangle .0 \mid \overline{w}. \langle \text{walk}' \rangle .0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle .0 \mid \overline{in}. \text{into}' .0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) .0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle .0$$

How SGIA works:

- the referring expression “this winding street”

$$\underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. nw' \langle \lambda u (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, u)) e) \langle \langle \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) \rangle \rangle \rangle .0$$

$$= \underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. nw' \langle (\lambda x (\text{walk}'(x, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) e \rangle .0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \lll (\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \ggg . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- event introduction:

$$\underline{nw} (nw'). \overline{pr}. nw' \lll (\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \ggg . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. nw' \langle \langle \langle \text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))) \rangle \rangle \rangle . 0 \mid \overline{w}. \langle \leftarrow \text{walk}' \rightarrow \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- Resulting term: $(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))))$ is the proposition
- “now”: $\overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0$ looks for and with which it combines to yield another proposition:

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle .0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. \lambda p \text{now}'(p) \langle \langle \langle \text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))) \rangle \rangle \rangle .0 \mid \overline{w}. \langle \text{walk}' \rangle .0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle .0 \mid \overline{in}. \text{into}' .0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) .0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle .0$$

How SGIA works:

$$\overline{n}. \langle \lambda p \text{now}'(p) \rangle .0$$

$$\underline{nw} (nw'). \overline{pr}. \lambda p \text{now}'(p) (\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) .0$$

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“Street” solution

$SGIA =_{\text{def}} !\bar{f}b. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \underline{w}e (we'). \langle \lambda p (\text{well}'(p))(we') \rangle .0 \mid \underline{w}$
 $(w'). \underline{i} (i'). \underline{ts} (ts^t). \underline{nw} (nw'). \bar{p}r. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x)$
 $\wedge \text{winding}'(x))) \rangle .0 \mid \bar{w}. \langle \text{walk}' \rangle .0 \mid \bar{n}. \langle \lambda p \text{now}'(p) \rangle .0 \mid \bar{i}n. \text{into}' .0 \mid \underline{s} (s'). \bar{ts}.$
 $\text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)).0 \mid \underline{b} (b'). \bar{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle .0$

How SGIA works:

$\bar{n}. \langle \lambda p \text{now}'(p) \rangle .0$

$\underline{nw} (nw'). \bar{p}r. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge$
 $\text{winding}'(x))) \rangle .0$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))) \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \underline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)). 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

- New proposition: put on an outgoing channel, combines with “well”, again generating a proposition:

$$\overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))) \rangle . 0$$

$$\underline{we} (we'). \langle \lambda p (\text{well}'(p))(we') \rangle . 0$$

$$= \langle \lambda p (\text{well}'(p)) (\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle . 0$$

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“Street” solution

$$\text{SGIA} =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle . 0 \mid \underline{we} (we'). \langle (\text{well}'(\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))))) \rangle . 0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts'). \underline{nw} (nw'). \overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle . 0 \mid \overline{w}. \langle \text{walk}' \rangle . 0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle . 0 \mid \overline{in}. \text{into}' . 0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)) . 0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle . 0$$

How SGIA works:

$$\overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle . 0$$

$$\underline{we} (we'). \langle \lambda p (\text{well}'(p)) (we') \rangle . 0$$

$$= \langle \lambda p (\text{well}'(p)) (\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle . 0$$

$$(\text{well}'(\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))))) . 0$$

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“Street” solution

$$\begin{aligned} \text{SGIA} =_{\text{def}} & \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \underline{we} (we'). \langle (\text{well}'(\text{now}'(\text{walk}'(e, \\ & \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))))) \rangle .0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts^t). \underline{nw} \\ & (nw'). \overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle .0 \mid \\ & \overline{w}. \langle \text{walk}' \rangle .0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle .0 \mid \overline{in}. \text{into}' .0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \\ & \text{winding}'(x)).0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle .0 \end{aligned}$$

How SGIA works:

- winding gesture continues to be held. So we have at the end of the process communication:

$$\overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \text{well}'(\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(e, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))))).0 \mid$$

$\mid .0$ null-agent due to propositional function

$\mid .0$ null-agent due to walk'

$\mid .0$ null-agent due to now'

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“Street” solution

$SGIA =_{\text{def}} \overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \underline{we} (we'). \langle (\text{well}'(\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))))) \rangle .0 \mid \underline{w} (w'). \underline{i} (i'). \underline{ts} (ts^t). \underline{nw} (nw'). \overline{pr}. \langle \text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)))) \rangle .0 \mid \overline{w}. \langle \text{walk}' \rangle .0 \mid \overline{n}. \langle \lambda p \text{now}'(p) \rangle .0 \mid \overline{in}. \text{into}' .0 \mid \underline{s} (s'). \overline{ts}. \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x)).0 \mid \underline{b} (b'). \overline{s}. \langle \lambda u (\text{street}'(u) \wedge \text{winding}'(u)) \rangle .0$

$\overline{!fb}. \langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle .0 \mid \text{well}'(\text{now}'(\text{walk}'(e, \text{you}') \wedge \text{into}'(x, \text{this}' x (\text{street}'(x) \wedge \text{winding}'(x))))).0 \mid$

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Cooper's Conjecture: Event Reading Idea

Idea:

Gesture is modifying the event in the propositional function

Consequences:

- Extend the propositional function
- Change the type of the gesture channel
- Change the speech-gesture contact point (interacting earlier on)

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Cooper's Conjecture: Event Reading Idea

$$\text{SGIA} =_{\text{def}} \overline{\text{fb}}. \langle \lambda u(\text{winding}'(u)) \rangle.0 \mid \underline{\text{we}} (\text{we}'). \langle \lambda p(\text{well}'(p))(w') \rangle.0 \mid \underline{\text{wind}}(\text{wind}').$$

$$\underline{\text{w}} (w'). \underline{\text{i}} (\text{i}'). \underline{\text{ts}} (\text{ts}'). \underline{\text{nw}} (\text{nw}'). \overline{\text{pr}}. \text{nw}' \langle \langle \langle \lambda g \text{fru} \exists e (f'(e, \text{you}') \wedge r(e, u) \wedge g(e))$$

$$\text{wind}')w' \rangle \text{i}' \rangle \text{ts}' \rangle.0 \mid \overline{\text{w}}. \langle \text{walk}' \rangle.0 \mid \overline{\text{n}}. \langle \lambda p \text{now}'(p).0 \rangle \mid \overline{\text{in}}. \text{into}' \mid \underline{\text{s}}(\text{s}'). \underline{\text{ts}}. \langle \langle \lambda g$$

$$(\text{this } x (g(x)) \text{ s}') \rangle.0 \mid \underline{\text{b}}(\text{b}'). \overline{\text{s}}. \langle \text{b}' \langle \lambda x(\text{street}'(x)) \rangle \rangle.0$$

Winding' sends its information via $\overline{\text{fb}}$ and $\underline{\text{wind}}$

- to the event e in the propositional function
- $\lambda g \text{fru} \exists e (f'(e, \text{you}') \wedge r(e, u) \wedge g(e)) \text{wind}')w' \rangle \text{i}' \rangle \text{ts}' \rangle.0$ and
- a winding event $\text{winding}'(e)$ is created.

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Modelling of Context

Contexts are called “environments”. $\Psi \triangleright P \xrightarrow{\alpha} P'$

In an environment that asserts Ψ P can perform an action α leading to P' .

“ \triangleright ” behaves similar to Situation Semantic’s “ \models ”.

Environmental assertions Ψ express effect of environment upon agent:

- conditions on agents and channels
- enabling interactions between parallel agents
- enabling conditions for case

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Structural Operational Semantics for Parallel Agents Reconsidered

First step in derivation of example:

$$\Psi \otimes \Psi_P \otimes \Psi_Q \vdash fb \leftrightarrow b$$

$$\Psi_Q \otimes \Psi \triangleright P \xrightarrow{\overline{fb}(\langle \lambda f \lambda u (f(u) \wedge \text{winding}'(u)) \rangle)} P' \Psi_P \otimes \Psi \triangleright Q \xrightarrow{\underline{b}(b').\bar{s}.\langle b' \langle \text{street}'(x) \rangle \rangle} Q'$$

$$\Psi \triangleright P|Q \xrightarrow{\tau} P'|Q'$$

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Exploiting Non-determinacy

Assume gesture attachment as indicated in the intuitive syntax picture, i.e. the winding gesture can go with

- “street”
- with the preposition “into”
- or (by Cooper’s Conjecture) with the whole event as expressed in the propositional function

then we can use the case construct to express non-determinacy.

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Exploiting Non-determinacy

Assume for simplicity that $\varphi_i \top$, so all readings are equally probable.

Then we could have

Case T: SGIA_{street}
 T: SGIA_{into}
 T: SGIA_e

Gesture representation and channel conditions would have to be adjusted accordingly. Observe that we get different agents.

Also possible: Rank the φ_i s.

- Probabilistic extensions of process algebras
- Process algebras using priorities.

Contents

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Conclusion and Suggestions for Further Research

How to fit in dialogue:

Sketch of how to treat back-channels as agents/processes.

Example from Esghi, Howes, Gregoromichelaki, Hough, and Purver (2015):

A: The doctor

B: Chorlton?

A: No, Fitzgerald.

B: uh-huh.

A: he examined me.

- We have a clarification dialogue for the reference of “the doctor”.
- We need A- and B-processes, which are allowed to interact i-o-wise.
 - We have to make sure that we get alternating dialogue contributions.

Conclusion and Suggestions for Further Research

A	B
$\overline{\text{Out.}} \langle \iota x \exists s(\text{doctor}'(x, s)) \rangle$	$\underline{\text{In.}} \text{ thd.}$ case: $(d \in D_B = \text{thd}): \overline{\text{Out.}} \langle \text{"mhm"} \rangle .0$ $\neg (d = \text{thd}): \overline{\text{Out.}} \langle ?(\text{Chorlton} = \text{thd}) \rangle$
$\underline{\text{In.}} \text{ repl.}$ case: repl = "mhm": $\overline{\text{Out.}} \langle \lambda x (\text{he} = x \wedge \text{examined}(x, A)) \rangle .0$ repl = $?(Chorlton = \text{thd})$: case: $\iota x \exists s(\text{doctor}'(x, s)) = \text{Chorlton}$: $\overline{\text{Out.}} \langle \text{"mhm"} \rangle .0$ $\neg (\iota x \exists s(\text{doctor}'(x, s)) = \text{Chorlton})$. $\overline{\text{Out.}} \langle \text{"no"} \rangle .0$	$\underline{\text{In.}} \text{ rep.}$ case: $(\text{rep} = \text{"no"}): \neg (\text{Chorlton} = \text{thd})$
$\overline{\text{Out.}} \langle \iota x \exists s(\text{doctor}'(x, s)) = \text{Fitzgerald} \rangle$	$\underline{\text{In.}} \text{ thd.}$ case: $\iota x \exists s(\text{doctor}'(x, s)) = \text{Fitzgerald}$. $\overline{\text{Out.}} \langle \text{"uh-huh"} \rangle$
$\underline{\text{In.}} \text{ repl.}$ case: repl = "uh-huh": $\overline{\text{Out.}} \langle \lambda x (\text{he} = x \wedge \text{examined}(x, A)) \rangle .0$	

Conclusion and Suggestions for Further Research

- Grounding (including larger context) would have to be achieved *via* a common-belief and individual-belief model and a domain D starting with CPs A, B and the doctor (all done incrementally).
- Observe that a generalization is still missing here:
It would have to be “reference resolution” or some such using a mechanism like
 - R. Cooper’s IntegrateOwn/OtherAcknowledgement or
 - J. Ginzburgh’s QUD

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